## A Useful Relationship for the Differential Scanning Calorimetry Determination of Phase Purity in Partially Phase Mixed Copolymers

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This paper reports the derivation of a useful relationship (eq 4) for the quantitative differential scanning calorimetry (DSC) determination of soft- and hard-segment purity without restricting the value of the hard-segment change in heat capacity ( $\Delta C_p^H$ ).

DSC has been shown to be a useful tool in the determination of microphase separation, and there are a number of papers that detail the methods of obtaining the weight fraction of soft segment in the soft phase  $(M_{\rm SS})$  from Wood's or Fox's equations.<sup>1,2</sup> However, determination of  $M_{\rm SS}$  alone provides no information about the hard phase.

Camberlin and Pascault introduced a method of determining the soft-segment segregation (SRs):<sup>3-6</sup>

$$SR_{S} = (\Delta C_{p}^{\text{obs}} / W_{S}) / \Delta C_{p}^{S}$$
 (1)

where  $\Delta C_p^{\text{obs}}/W_{\text{S}}$  represents the observed change in heat capacity per gram of soft segment in the copolymer and where  $\Delta C_p^{\text{S}}$  represents the change in heat capacity of the ideally microphase-separated soft segment (see Glossary of Terms). By combining these two methods a complete description of the microphase separation behavior can be obtained, thereby providing information about the soft and hard phases.<sup>7</sup>

Camberlin and Pascault admit that because the contribution to  $\Delta C_p^{\text{obs}}$  by the excluded hard segments is ignored, eq 1 is applicable only in situations in which  $\Delta C_p^H$  is almost zero. Situations where this is not true can easily arise, and given the availability of DSC analysis, it is desirable to use DSC to obtain a quantitative evaluation of the microphase separation in these situations as well.

The formation of microphases occurs in block and segmented copolymers in which differing segments are incompatible, such as poly(urethane ethers) and poly(ester ethers). In the case of a segmented copolymer containing hard and soft segments, crystallization can provide an additional driving force for phase separation if semicrystalline hard phases can form. Unfortunately, microphase separation often is thought to involve the formation of nearly pure semicrystalline hard phases which are found in an amorphous matrix consisting of soft segments and excluded hard segments.8-11 Where this is true, a good description of the microphase separation can be obtained solely by determination of  $M_{SS}$ . A high degree of hard-segment purity is indicated by crystalline melting points that are equal to the melting point of the hard-segment homopolymer.<sup>1,2,13</sup> Other materials contain hard phases that are not pure since they exhibit melting points that are much lower than the melting point of the hard-segment homopolymer.<sup>3-7</sup> In these materials phase mixing of soft segments into the semicrystalline hard phase is an equally important consideration.

 $\hat{S}R_S$  is defined as the weight fraction of soft segment in the soft phase with respect to the total weight of soft segment in the copolymer—this parameter is termed a rate in the original treatment due to the time dependence of microphase separation.<sup>3-7</sup>  $SR_S$  is related to  $M_{SS}$  by the

equation

$$SR_S = M_{SS}W_{SP}/W_S \tag{2}$$

where  $W_{\rm SP}$  represents the weight fraction of the soft phase and where  $W_{\rm S}$  represents the weight fraction of the soft segment in the copolymer.

One can account for contributions to  $\Delta C_p^{\rm obs}$  from both the soft and hard segments by using the generally accepted principle that the observed change in heat capacity of a single-phase two-component system is the linear weighted addition of the two individual component changes in heat capacities. Applying this relation to a fully amorphous soft phase yields the equation 1

$$\Delta C_p^{\text{ obs}}/W_{\text{SP}} = M_{\text{SS}} \Delta C_p^{\text{ S}} + (1-M_{\text{SS}}) \Delta C_p^{\text{ H}} \qquad (3)$$

where  $\Delta C_p^{\rm obs}/W_{\rm SP}$  represents the observed change in heat capacity per gram of the soft phase. Unfortunately,  $W_{\rm SP}$  cannot be directly determined by DSC, but given eq 2 and 3, SR<sub>S</sub> can be determined by the relationship

$$SR_{S} = \frac{M_{SS}\Delta C_{p}^{\text{ obs}}/W_{S}}{M_{SS}\Delta C_{p}^{S} + (1 - M_{SS})\Delta C_{p}^{H}}$$
(4)

With eq 4 analysis can be extended beyond  $M_{\rm SS}$  by the calculation of SR<sub>S</sub> without restricting the value of  $\Delta C_p^{\rm H}$ , provided that suitable data are obtained from model compounds for the ideally microphase-separated hard and soft phases ( $\Delta C_p^{\rm H}$  and  $\Delta C_p^{\rm S}$ , respectively).

The conditions for which eq 1 is valid become obvious when it is realized that eq 4 reduces to eq 1 if the following approximation is allowed:

$$M_{\rm SS}\Delta C_p^{\rm S} + (1 - M_{\rm SS})\Delta C_p^{\rm H} \approx M_{\rm SS}\Delta C_p^{\rm S}$$
 (5)

Thus, eq 5 dictates the condition that permits the use of eq 1 for the determination of SR<sub>S</sub>. This condition is met by any of the following circumstances: (1)  $\Delta C_p^H$  is small such that  $\Delta C_p^S \gg \Delta C_p^H$  or (2) the sample is substantially microphase separated such that  $M_{\rm SS} \gg (1-M_{\rm SS})$ .

When none of these situations apply and  $\Delta C_p^{\rm H}$  is known, SR<sub>S</sub> can still be determined by eq 4. Further, because eq 4 takes into account the contributions of both components to  $\Delta C_p^{\rm obs}$ , its application is not limited to the hard segmentsoft segment combination. It also applies to other combinations, including soft segment—soft segment combinations, such as poly(siloxane ethers), of which there is an increasing interest. 14

Once both  $M_{\rm SS}$  and  ${\rm SR_S}$  are known, it is a simple matter to determine the composition of the hard phase. Assuming that only two phases are formed, the weight fraction of the hard segment in the hard phase  $(M_{\rm HH})$  can be estimated:<sup>3,7</sup>

$$M_{\rm HH} = 1 - [M_{\rm SS}W_{\rm S}(1 - {\rm SR_S})/(M_{\rm SS} - {\rm SR_S}W_{\rm S})]$$
 (6)

Furthermore, similar to  $SR_S$ , the hard-segment segregation ( $SR_H$ ) is calculated by the equation  $^7$ 

$$SR_{H} = (M_{SS}M_{HH} - SR_{S}W_{S}M_{HH})/M_{SS}W_{H}$$
 (7)

where  $W_{\rm H}$  represents the weight fraction of the hard segment in the copolymer.

The strength of this process lies in its ability to produce a complete description of the microphase separation behavior, providing information about the soft and hard phases. By use of these equations, a complete description of phase purity can be obtained by DSC analysis for a wider variety of microphase-separated materials.

## Glossary of Terms

| $\Delta C_p^{ m obs}$     | observed change in specific heat capacity of the<br>soft phase in the copolymer per unit mass of<br>copolymer  |
|---------------------------|--|
| $\Delta C_{ ho}{}^{ m H}$ | change in specific heat capacity of the ideally mi-<br>crophase-separated hard phase per unit mass of<br>pure-component material                     |
| $\Delta C_p$ S            | change in specific heat capacity of the ideally mi-<br>crophase-separated soft phase per unit mass of<br>pure-component material                     |
| $SR_S$                    | soft-segment segregation; weight fraction of soft<br>segments in the soft phase with respect to the<br>total weight of soft segment in the copolymer |
| $SR_H$                    | hard-segment segregation; weight fraction of hard<br>segments in the hard phase with respect to the<br>total weight of hard segment in the copolymer |
| $W_{ m S}$                | weight fraction of the soft segment in the copolymer   |
| $W_{H}$                   | weight fraction of the hard segment in the copol-<br>ymer  |
| $W_{ m SP}$               | weight fraction of the soft phase  |
| $M_{ m SS}$               | weight fraction of soft segments in the soft phase   |
| $M_{ m HH}$               | weight fraction of hard segments in the hard phase   |
|                           |  |

## References and Notes

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